| Class: <br> Date: | Indian School Al Wadi Al Kabir  <br> Assessment 1 (2022-2023)  <br> Sub: MATHEMATICS(041) Max Marks: 80 <br> Time: 03 hrs. |
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| General Instructions: <br> 1. This question paper contains two sections - $A$ and $B$. Each part is compulsory. <br> 2. Section - A has 24 Objective type questions of 1 mark each and two case study-based questions of 4 marks each. <br> 3. Section - $\mathbf{B}$ has $\mathbf{0 8}$ questions of $\mathbf{0 2}$ marks, $\mathbf{0 4}$ questions of $\mathbf{0 3}$ marks and $\mathbf{0 4}$ questions of $\mathbf{0 5}$ marks. <br> 4. Internal choice has been provided. |  |
| SECTION A (1mark) |  |
| Q1. | List all the elements of the set $A=\left\{x: x^{2} \leq 4, x \in Z\right\}$ |
| Q2. | In a school there are 20 teachers who teach mathematics or physics. Of these, 12 teach mathematics and 4 teach both physics and mathematics. How many of them teach physics? <br> OR <br> A market research group conducted a survey of 1000 consumers and reported that 720 consumers like product A and 450 consumers like product B , what is the least number that must have liked both products? |
| Q3. | Write $\mathrm{P}(\mathrm{A})$ if $\mathrm{A}=\{1,2\}$. |
| Q4. | Write the set builder form of $A=\{2,4,6,8,10\} \quad$ OR $\mathrm{A}=\{1,2,3\}$ and $B=\{3,4,5\}$ then write $(A-B) U(B-A)$ |
| Q5. | How many relations can be defined from $A$ to $B$ if $n(A)=3$ and $n(B)=2$. |
| Q6. | Write the domain of the real valued function $\mathrm{f}(\mathrm{x})=\frac{2 \mathrm{x}+1}{\mathrm{x}^{2}-9}$. |
| Q7. | If $A=\{5,6\}$ and $B=\{6,8,10\}$ then write $B \times A$. |
| Q8. | If $\mathrm{R}=\{(x, 2 x-1): x=0,1,2,3\}$, then write R in roster form. |
| Q9. | Evaluate: $\cos 480^{\circ}$ <br> Convert 2.2 radians to degree measure. ( $\pi=\frac{22}{7}$ ) <br> OR |
| Q10. | Evaluate: $\cot \left(\frac{19 \pi}{4}\right)$. |



| Q22. | Which of the following relations are functions? |  |  |  |  |  |  |  |
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|  | A | $i$ and ii | B | ii and iv | C | i, ii, iii and iv | D | none of these |
| Q23. | Range of the function $f(x)=\frac{x^{2}}{x^{2}+1}$ |  |  |  |  |  |  |  |
|  | A | $\{1,2\}$ | B | $[0, \infty)$ | C | $[0,1)$ | D | $(-\infty, 1)$ |
| Q24. | The domain and range of the function $f(x)=\sqrt{9-x^{2}}$ |  |  |  |  |  |  |  |
|  | A | $\begin{gathered} \text { Domain: }[0,3] \\ \text { Range: }[0,3] \end{gathered}$ | B | $\begin{aligned} & \text { Domain: }[-3,3] \\ & \text { Range: }[0,3] \end{aligned}$ | C | Domain: $\{0,3\}$ <br> Range: $\{0,3\}$ | D | $\begin{gathered} \text { Domain: }\{-3,3\} \\ \text { Range: }\{0,3\} \end{gathered}$ |
|  | Section A-Case Study based questions |  |  |  |  |  |  |  |
| Q25. | CASE STUDY QUESTIONS <br> In a group of 50 students, the number of students studying Physics, Biology and Mathematics were found to be as follows. Physics - 17, Biology - 13, Mathematics - 15, Physics and Biology - 9, Biology and Mathematics - 4, Physics and Mathematics - 5, All three subjects - 3 . <br> Based on the above information answer the following questions. <br> (ANSWER ANY FOUR QUESTIONS) |  |  |  |  |  | - |  |
|  | Find the number of students <br> i) who study none of the three subjects. <br> A) 20 <br> B) 27 <br> C) 30 <br> D) 10 <br> ii) who study Physics and Biology but not Mathematics. <br> A) 9 <br> B) 12 <br> C) 6 <br> D) 10 <br> iii) Who study exactly one of the subjects. <br> A) 30 <br> B) 20 <br> C) 21 <br> D) 18 <br> iv) Who study at least one of the subjects. <br> A) 37 <br> B) 30 <br> C) 20 <br> D) 34 <br> v) Who study exactly two of the three subjects. <br> A) 3 <br> B) 12 <br> C) 8 <br> D) 9 |  |  |  |  |  |  |  |


| Q26. | Sherlin and Danju are playing Ludo. While rolling the dice, Sherlin's sister Raji observed and noted the possible outcomes of the throw every time belongs to set $\{1,2,3,4,5,6\}$. Let $A$ be the set of players while $B$ be the set of all possible outcomes. <br> Answer the following questions based on the above informations: |
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|  | a. Let R be a relation from B to B such that $\mathrm{R}=\{(\mathrm{a}, \mathrm{b})$ : a divides $\mathrm{b}, \mathrm{a}, \mathrm{b} \in B\}$. Write R in roster form. <br> b. Is the relation R a function? Why? Justify your answer. |
|  | SECTION B (2marks) |
| Q27. | Let $A$ and $B$ are two finite sets such that $n(A)=m$ and $n(B)=n$. If the difference of number of subsets of A and B is 120 , find the values of m and $\mathrm{n} .(m>n)$ |
| Q28. | Solve: $\|x-2\| \leq 3 \quad$ OR $\quad$ Solve: $\frac{x}{3}+\frac{x}{4}+x<19$ |
| Q29. | If $A=\{0,1,2,3,4,5\}$ and a relation $R$ is defined as <br> $R=\{(x, y): x, y \in A, x+y>7\}$. Express the relation as set of ordered pairs and determine the domain and range of R . |
| Q30. | The water acidity in a pool is considered normal when the average $\mathrm{p}^{\mathrm{H}}$ reading of three daily measurements is between 8.2 and 8.5.If the first two readings are 8.4 and 8.3 then find the range of $\mathrm{p}^{\mathrm{H}}$ value for the third reading that will result in the acidity level being normal. |
| Q31. | For three sets $\mathrm{A}, \mathrm{B}$ and C shade the following using a Venn diagram: $(A \cap B U C)$ <br> OR <br> If $A$ and $B$ are two sets containing 3 elements and 6 elements respectively. What can be the maximum number of elements in AUB? Find also the minimum number of elements in AUB. |
| Q32. | Write the domain and range of the function $f(x)=\|x\|-2$ |
| Q33. | Prove: $\frac{\boldsymbol{\operatorname { t a n }}\left(\frac{\pi}{4}+\mathrm{x}\right)}{\boldsymbol{\operatorname { t a n }}\left(\frac{\pi}{4}-\mathrm{x}\right)}=\left(\frac{1+\boldsymbol{\operatorname { t a n } x}}{1-\boldsymbol{\operatorname { t a n } x}}\right)^{2}$. <br> OR <br> Prove: $\tan 3 \mathrm{x} \tan 2 \mathrm{x} \tan \mathrm{x}=\tan 3 \mathrm{x}-\tan 2 \mathrm{x}-\tan \mathrm{x}$ |
| Q34. | Find all pairs of consecutive odd natural numbers, both of which are larger than 10, such that their sum is less than 29. |


|  | SECTION B (3marks) |
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| Q35. | $\mathrm{A}, \mathrm{B}$ and C are three sets defined as $A=\left\{x: x^{2}+x-6=0\right\}, B=\{x: 1<x<4, x \in N\}$ and $C=\{x: x$ is a prime number less than 5$\}$. Determine which of the sets $\mathrm{A}, \mathrm{B}$ and C are equal. Why? |
| Q36. | Prove: $\cos \left(\frac{3 \pi}{2}+x\right) \cos (2 \pi-x)[\tan x+\cot x]=1$ <br> OR <br> Evaluate: $\tan \frac{\pi}{8}$. |
| Q37. | Prove that $2 \cos \frac{\pi}{13} \cos \frac{9 \pi}{13}+\cos \frac{3 \pi}{13}+\cos \frac{5 \pi}{13}=0 \quad$ OR <br> If $\tan A=\frac{3}{4}, A \in$ III Quadrant, then evaluate $\sin \frac{A}{2}$. |
| Q38. | In an experiment, a solution of hydrochloric acid is to be kept between $30^{\circ}$ and $35^{\circ}$ Celsius. What is the range of temperature in degree Fahrenheit if conversion formula is given by $C=\frac{5}{9}(F-32)$, where C and F represent temperature in degree Celsius and degree Fahrenheit, respectively. |
|  | Section B (5 Marks) |
| Q39. | Solve the inequalities and represent the solution on number line: $2(2 x+3)-10<6(x-2) ;\left(\frac{x-7}{2}\right) \leq 10-x$ |
| Q40. | $\begin{aligned} & U=\{0,1,2,3, . .10\}, \quad A=\{2,3,4,5\}, B=\{3,5,7,9\}, C=\{1,3,5,7,9\} . \\ & \text { Find (i) }(A \cap B)^{\prime}, \quad \text { (ii) } A-(B \cup C), \quad \text { (iii) }(A-B) U(B-C) . \\ & \text { Verify }: A \cup(B \cap C)=(A \cup B) \cap(A \cup C) \end{aligned}$ |
| Q41. | If $f$ and $g$ are real valued functions defined as $f(x)=x^{2}+7, g(x)=3 x+5$. Then evaluate each of the following: <br> i) $f(-3)+g(-5)$ <br> ii) $f(g(-1))$ <br> iii) $g(f(0))$ <br> iv) $f(0)-g\left(\frac{2}{3}\right)$ <br> v) $\frac{f(t)-g(1)}{t-1}, t \neq 1$ |
| Q42. | Prove: $\frac{\sin A+\sin 3 A+\sin 5 A+\sin 7 A}{\cos A+\cos 3 A+\cos 5 A+\cos 7 A}=\tan 4 A$ <br> OR <br> Prove: $\cos ^{2} x+\cos ^{2}\left(x+\frac{\pi}{3}\right)+\cos ^{2}\left(x-\frac{\pi}{3}\right)=\frac{3}{2}$. |

